

GANPAT UNIVERSITY
B.TECH SEM-IV ELECTRICAL ENGINEERING
REGULAR EXAMINATION MAY-JUNE-2013
2EE404:-COMPUTER ORIENTED NUMERICAL METHODS

Time: 3 Hours

Total Marks:-70

- Instructions:** - 1. Attempt all questions.
 2. Make suitable assumptions wherever necessary.
 3. Figures to the right indicate full marks.

SECTION-I

- Q:1 (A)** Fit a least square curve of the form $y = a x^b$ for the following data: (6)
 Where a and b are constants

x:	61	26	7	2.6
y:	350	400	500	600

- (B)** (i) Prove that $\delta = \Delta E^{-1/2}$ and hence prove that $E = \left(\frac{\Delta}{\delta}\right)^2$. (6)
 (ii) $\Delta^{10}[(1-x)(1-2x^2)(1-3x^3)(1-4x^4)] =$ _____

OR

- Q:1 (A)** From the data given below, find the number of students whose weight is between 60 to 70. (6)

Weight	0-40	40-60	60-80	80-100	100-120
No. of students	250	120	100	70	50

- (B)** A thermocouple gives the following output for rise in temperature: (6)

Temp(°C)	0	10	20	30	40	50
Output(mV)	0.0	0.4	0.8	1.2	1.6	2.0

Find the output of thermocouple for 37 °C temperature using Newton's Divided difference formula.

- Q:2 (A)** Find all the Eigen values & Eigen vectors of the matrix (6)

$$\begin{vmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{vmatrix}$$

- (B)** Solve the equations (5)
 $10x+2y+z=9$; $2x+20y+2z=-44$; $-2x+3y+10z=22$, by using Jacobi's method.

OR

- Q:2 (A)** Solve the equations, (6)
 $10x-2y+z=12$; $x+9y-z=10$; $2x-y+11z=20$, by using gauss elimination Relaxation method.

- (B)** Show that the following systems of equations are ill-conditioned or not? (5)
 $3x_1 + x_2 = 9$; $3.015x_1 + x_2 = 3$

- Q:3** **Attempt any two:** (12)

- (A)** Using the finite difference method, find $y(0.025)$, $y(0.5)$, $y(0.75)$ satisfying the differential equation $\frac{d^2y}{dx^2} + y = x$, subject to the boundary conditions $y(0)=0$, $y(1)=2$.

- (B)** Construct the table of differences for the data:

X:	0	1	2	3	4
F(x):	1.0	1.5	2.2	3.1	4.6

Evaluate $\Delta^3 f(2)$.

- (C)** What are the basic sources of errors in numerical computation? Explain with suitable block diagram.

SECTION-II

Q:4 (A) Solve $dy/dx=y^2+x, y(0)=1$ using Taylor's series method and compute $y(0.1)$ and $y(0.2)$ (6)

(B) Use the iterative method, find the inverse of (6)

$$A = \begin{pmatrix} 1 & 10 & 1 \\ 2 & 0 & 1 \\ 3 & 3 & 2 \end{pmatrix} \text{ taking } B = \begin{pmatrix} 0.4 & 2.4 & -1.4 \\ 0.14 & 0.14 & -0.14 \\ -0.85 & -3.8 & 2.8 \end{pmatrix}$$

OR

Q:4 (A) Using the finite difference method, find $y(0.025), y(0.5), y(0.75)$ satisfying the differential equation $\frac{d^2y}{dx^2} + y = x$, subject to the boundary conditions $y(0)=0, y(1)=2$. (6)

(B) Write and explain the two limitations of Newton-Raphson method. (6)

Q:5 (A) Find the value of $\cos 1.74$ using the table given below: (6)

X:	1.70	1.74	1.78	1.82	1.86
Sin x:	0.9916	0.9857	0.9781	0.9691	0.9584

(B) Evaluate the real root of the equation $x - \cos x = 0$, by using bisection method. (5)

OR

Q:5 (A) Find $\int_0^6 \frac{e^x}{1+x} dx$ using Simpson's 1/3rd rule. (6)

(B) Given that $\frac{dy}{dx} = \frac{y-x}{y+x}$ with initial conditions $y=1$ at $x=0$; find y for $x=0.1$ by Euler's rule. (5)

Q:6 Attempt any two: (12)

(A) (i) Classify the equation $(1+x^2) \frac{\partial^2 u}{\partial x^2} + (5+2x^2) \frac{\partial^2 u}{\partial x \partial t} + (4+x^2) \frac{\partial^2 u}{\partial t^2} = 0$
 (ii) Define absolute, relative and percentage errors. Illustrate each of them with suitable examples.

(B) From the following data:

X:	1.8	2.0	2.2	2.4	2.6
Y:	2.9	3.6	4.4	5.5	6.7

Find x when $y=5$ using iterative method.

(C) Using Euler-Maclaurin formula, find the value of $\log_e 2$ from $\int_0^1 \frac{dx}{1+x}$

END OF PAPER

Best of Luck